# CALIFORNIA INSTITUTE OF TECHNOLOGY 

Selected Topics in Computer Science and Economics

## CS/EC/101b

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## Homework Set $\# 6$

All students should complete the following problems:

1. You are managing a start-up company and have an important decision to make. And once you make the decision you cannot reverse it. You need to choose one of two software designs, $A$ or $M$. The world only wants one of these but it is not obvious which. When you start the analysis you can only assume that $P(A)=P(B)=.5$. That is, there is an equal probability of $A$ or $B$. If you guess right, you will make a lot of money, $\$ 5,000,000$. If you guess wrong, you will only make $\$ 500,000$. But you can collect some data before you have to choose. Each piece of data costs $\$ 10,000$. Each piece of data is a signal, $a$ or $b$. The conditional probabability that $a$ occurs given $A$ is 0.6 , that is, $P(a \mid A)=.6$. Also, $P(a \mid B)=.4$.
(a) If you have to decide to get your data in one bunch (think batch process), how many pieces of data should you ask for? What is your decision rule for choosing $A$ or $B$ ? [The latter question is asking what you will do if you see $k a$ and $l b$ in the data.] ( 25 pts )
(b) Now suppose you can collect the data one piece at a time. Will you pay for the first piece? Why? Under what conditions would you stop after the first piece and choose $A$ or $M$ ? Under what conditions would you stop after two pieces? ( 25 pts )
[Extra credit: Can you figure out a general decision rule for this problem? That is can you solve for a function $d(k, t-k)$ where $t$ is the number of data pieces you have bought (paying $\$ 10,000$ for each), $k$ is the number of $a$ 's you have seen, and $d(k, t-k)=0$ if you will buy another data piece, $d(k, t-k)=A$ if you choose $A$ at this point, and $d(k, t-k)=B$ if you choose $B$ at this point]
2. A seller has an object she wants to sell with an auction. She is trying to decide whether to use a first price sealed bid auction or a second price sealed bid auction. She knows the following facts as do the bidders. There will be two bidders, $i=1,2$. Each bidder $i$ has a utility function of $v^{i}-p$ if they win, and have to pay $p$, and 0 if they don't win. Each $v^{i}$ is uniformly distributed on the interval $[0,100]$.
(a) Which auction, first price or second price, will yield more expected revenue? Why? (25 pts)
(b) Show that if she were to run a second price auction with an appropriate reserve price then she can increase her expected revenue. (25 pts)

Please, turn in the homework in the box outside Jorgensen Lab, 62.

